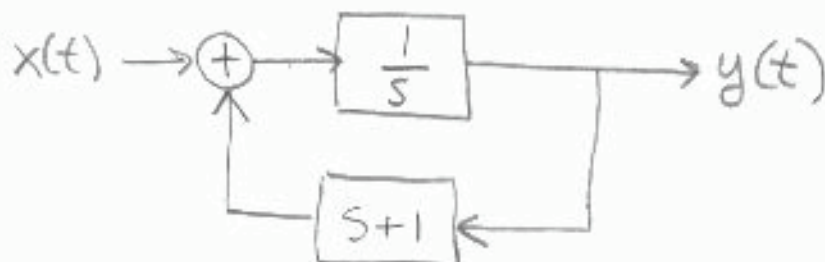


Question



write the differential equation for the system above.

Answer

The system response is

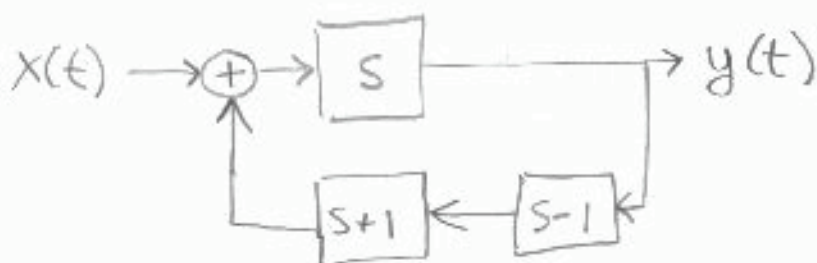
$$H(s) = \frac{\frac{1}{s}}{1 - (s+1)\frac{1}{s}} = \frac{1}{s - s + 1} = 1$$

$$2 \frac{dy(t)}{dt} - y(t) = x(t)$$

The negative sign is because $F(s) = -(s+1)$
where

$$\Rightarrow H(s) = \frac{G(s)}{1 + F(s)G(s)}$$

Question



using the standard formula for feedback, write the differential equation for the system above.

Answer

$$G(s) = s$$

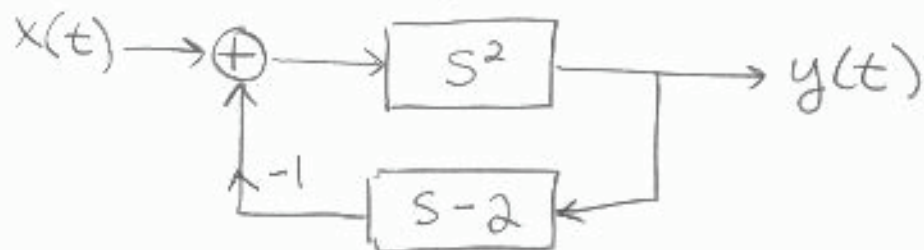
$$F(s) = -(s+1)(s-1) = -s^2 + 1$$

$$H(s) = \frac{s}{1 + s(-s^2 + 1)} = \frac{s}{1 - s^3 + s}$$

$$-\frac{d^3 y(t)}{dt^3} + \frac{dy(t)}{dt} + y(t) = \frac{dx(t)}{dt}$$

Question

Use the standard feedback equation to compute the Laplace transform of the following system.



write the differential equation for the above system

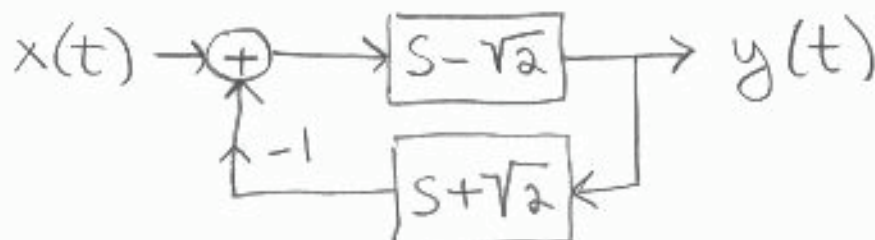
Answer

$$H(s) = \frac{G(s)}{1 + F(s)G(s)} = \frac{s^2}{1 + s^3 - 2s^2}$$

$$\frac{d^3 y(t)}{dt^3} - 2 \frac{d^2 y(t)}{dt^2} + y(t) = \frac{d^2 x(t)}{dt^2}$$

Question

What is the Laplace Transform for the following Feedback system



what differential equation governs this system?
plot the poles + zeros.
is it stable?

Answer

$$H(s) = \frac{G(s)}{1 + F(s)G(s)} = \frac{s - \sqrt{2}}{1 + s^2 - 2} = \frac{s - \sqrt{2}}{s^2 - 1}$$

$$= \frac{(s - \sqrt{2})}{(s - 1)(s + 1)}$$

